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The effect of perforations on the deformability of welded beam with corrugated webs

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Keywords: beam with corrugated web, web perforation; triangular shape of corrugations, beam deflection, finite element analysis, ring stiffener.

Abstract. Perforating steel beams is inevitable in some cases such as setting the technical equipment, though it decreases the carrying capacity of the element. The lack of information about the nature of the work, the values of critical stresses, the stability of the corrugated webs of the beams weakened by the perforations necessitated relevant studies for which the perforations of different diameters and with various ways of reinforcement were formed in the webs of the beams. Hence, this research focuses on the behavioral condition of welded beams with corrugated triangular webs weakened by different sized perforations at different locations. The impacts of these perforations on the transverse load-carrying capacity of the element and the suitable ways for stiffening them were investigated. An analysis is made of the influence of the edging thickness, paired vertical stiffeners at different widths of the ring stiffener on behavior of models of beams with a corrugated web with perforations. The influence of the bending of the lip around the exterior circumferential edge of the stiffener ring on the bearing capacity of beams with a corrugated web weakened by perforations was analyzed. The most effective location of the perforations along the web height has been determined.

1. Introduction

The main aim of this research directed on identification behavioral condition and deformability of welded beams with corrugated triangular webs weakened by perforations.

During this research the main tasks need to defined: 1) necessity of stiffening the web and the perforation; 2) the most optimal sized of perforations, distance between perforations and types of strengthening; 3) influence of a lip around the exterior circumferential edge of the stiffener ring on bearing capacity of the beam weakened by the perforations; 4) the most effective location of the perforation along the web height.

A Corrugated beam is a beam with flanges made of different section metal and corrugated (curved) web in transverse direction [1]. Corrugated webs of beams can be with a triangular corrugation profile [2], wavy, trapezoidal [3, 4], rectangular, etc. flanges of such beams are made of rolled steel, molded sections, electric-welded pipes, reinforced concrete elements. Beams with corrugated webs are used in many countries (Table 1).

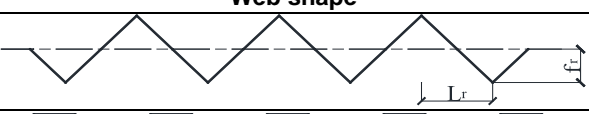


Literary sources with open access [5, 6] have a few solutions of the problems of designing perforations in the corrugated webs. There are also limited data on experimental and theoretical studies of influence of local concentrated loads and local weakening on the bearing capacity and deformation of beams. This question was mainly considered in thin-walled beams [7–13] and in beams with flat webs and with perforated webs [14, 15]. The need for perforations application in the corrugated webs is due to the fact that laying of the piping system for various purposes: water supply, heating, ventilation, air conditioning.

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Table 1. Area of application and corrugated web shape, where L_r is the length of the corrugation half-wave; f_r is the height of the corrugation half-wave.

Beam Name	Place of Application	Web shape
Beams with cross-corrugated web and triangular-shaped corrugations	Kazakhstan, Russia, Tajikistan	
Beams with corrugations of a trapezoidal and rectangular shape	Sweden, the USA, Japan, Finland	
Beams with cross-corrugated web and wavy-shaped corrugations	Austria, Ukraine, Poland, Russia	

The issues of the perforations affect the work of the beam web which are performed according to the Vierendeel principle or the four-angular bend [16], are studied in various works [17–19]. Also, the problems of placing and stiffening of perforations in the corrugated webs of trapezoidal and wavy shape of corrugations were solved in different countries by many scientists [20, 21]. However, except the study [16], for beams with a corrugated web and corrugations of a triangular shape no more study was revealed.

In view of the absence in the regulatory documents on the territory of the Republic of Kazakhstan and Russia a proper explanation of the pitch, diameter and methods of reinforcing perforations, there is a need to conduct a study of the influence of the diameter and pitch of perforations on the deformability of the corrugated beam, in order to develop a methodology for designing welded corrugated beams, weakened by perforations.

The stressed state of the corrugated web in the perforation zone is a separate issue requiring additional studies that take into account the ratio of the diameter of the perforations and the beam web height, the perforations pitch, the stiffness of the element supporting the shape of the perforation.

2. Methods

Experimental studies of corrugated beams are a very important part of the substantiation of various hypotheses about the principles of work and the effectiveness of the design decisions [22–26]. There are no specific requirements on the number, pitch and diameter of the perforations in both Kazakhstan and foreign building regulations.

The experimental study was performed on two support beams with a corrugated web with a triangular shape of the corrugations, without perforations and weakened by three perforations. Three circular perforations with a diameter of $0.5h_w$, where h_w is the web height (Figure 1), were provided to ensure the various types of communication passage in the beams webs. Since there is no exact method for calculating the corrugated beams with weakening, then the beams with thin corrugated webs weakened by perforations require appropriate field tests for the practical application in construction. The geometric parameters, materials, loads and boundary conditions adopted during the experiment are presented below.

As a result of theoretical and experimental studies carried out at the beginning of the 90s by the Institute “Proektstalkonstrukciya” [27] based in its own laboratories, the use of corrugated webs in girder structures has expanded significantly. The test was performed on large-scale models (scale 1:3) of corrugated beams of constant section (flange is 220×10 mm, web is 840×1.9 mm) with a span of 8400 mm. The first beam B-1 was accepted without perforations. Three circular perforations with a diameter of $0.5h_w$, which edges were reinforced with stiffeners made of strip steel with a cross section of 85×3 mm, are formed in the web of the second beam B-2. The maximum allowable deflection of the beam is assumed to be $1/220L$, and is equal to 38.2 mm.

In the perforation zone in four sections of the web, rectangular sockets of three electrical strain gauges with a base of 10 mm were glued along the length. The indications of electrical strain gauges were taken visually by a CTM-5 device, and were also output to Iskra-108D printer and to a punched tape for further processing by a computer. The load at the time of testing in the elastic stage of the beam behavior was measured using a DOSM-5 model dynamometer with an accuracy class of 1.5 and duplicated using M100 manometers. Displacements of beams in the plane of the load action were measured using PAO-6 deflectometer with a division value of 0.01 mm. The deflectometers measured the vertical displacement and were located in sections where the load was applied, as well as on supports. The general view of the beams and their geometric dimensions is given in Figure 1.

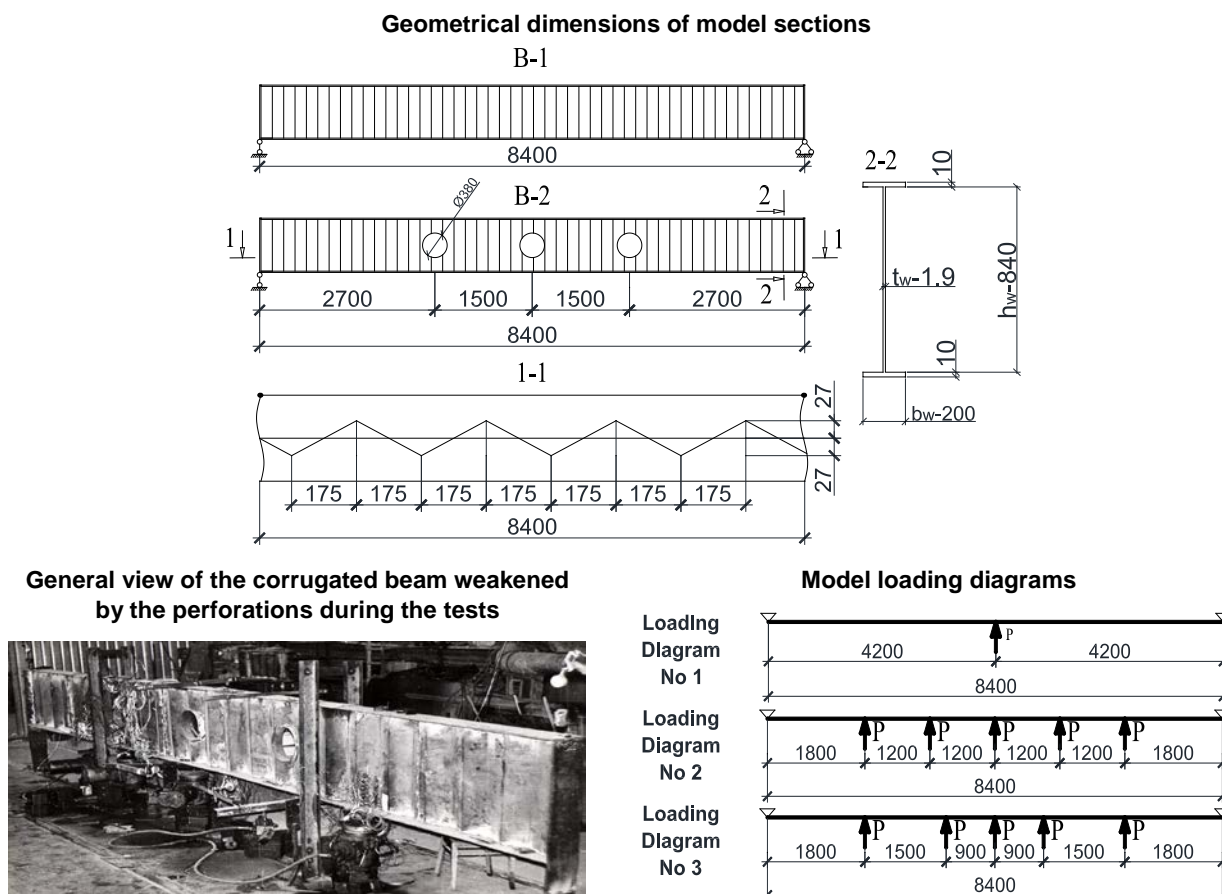


Figure 1. Data on the geometric dimensions of the model section, the general view of the beam during the tests and the tested models loading diagrams.

The web corrugations of triangular shape with roundings in the peaks had a wave length $L_r = 50$ mm and a wave height $f_r = 54$ mm. Material of the web and flanges was taken steel S245 in accordance with Russian State Standard GOST 27772 [28] with the following characteristics: yield strength $\sigma_y = 245$ N/mm² and ultimate strength $\sigma_u = 370$ N/mm². The Beams were made in the laboratory for metal structures testing. The general view of the corrugated beam weakened by the perforations, is given in Figure 2.

The beams were loaded with DGO 100/2/G50H A0CM5 hydraulic jacks through steel plates of 100×20 mm long equal to the width of the beam flange ($L = 200$ mm). To ensure equal loads jacks installed symmetrically relative to the middle of the beam, were connected by hoses and loaded manually with a single pump. Loading diagrams are shown in Figure 1.

The beams deformation property was also studied along with the study of the beam elements stressed state, since there is little information about the beams deformation property with thin corrugated webs, and especially weakened by perforations; and their interest in construction practice is special. The effect of local wall stability loss on the structure behavior was not taken into account in this work.

The performed tests make it possible to conduct a comparative analysis of the beams deformation property (Figure 2) of the same cross-section with perforations in the web and without such perforations under the same operating conditions, as well as to check the computer simulation data of the tests in the LIRA-SAPR 2017 software package with the aim of further usage of this program as the main one for further numerical investigations of the corrugated beam weakened by circular perforations of different pitch and diameter.

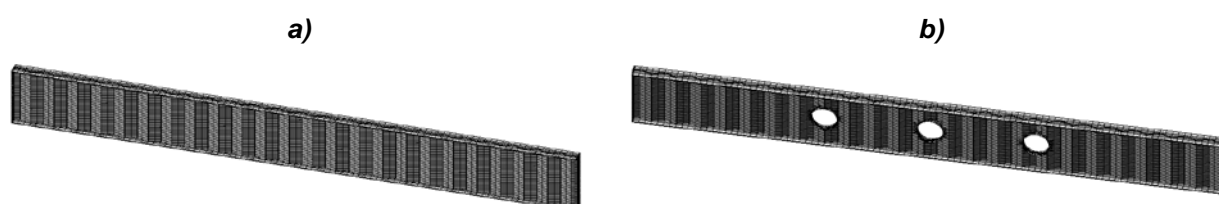


Figure 2. The model of beams: a) B-1; b) B-2.

Table 2 presents the values of the bending moments in the middle of the span M_e , the transverse force at the supports Q_e , the stresses in the flanges σ_{\max} , the stresses in the web τ_{\max} , as well as the experimental Y_e , theoretical Y_t and computer Y_c deflections of the B-1 beam without the perforations ones. The values of deflections in the middle of the B-2 beam with perforations for 1, 2 and 3 loading diagrams of experimental Y_e^* and computer Y_c^* data in the linear region of behavior are also presented. For the numerical experiment, the following grid was adopted: 0.04×0.09 m, in the area of the perforations, the grid is reduced to 2 times. Computer simulation of the beams was performed using the program LIRA-SAPR, program for the finite element analysis. The boundary conditions were applied to both ends of the beam model at the nodes of the end plate surface by limiting the required degrees of freedom. The beam at both ends has a fastening along the axes Y and Z . The material of the web and flanges is S245 steel in accordance with Russian State Standard GOST 27772 [28]. The yield strength is $\sigma_y = 245 \text{ N/mm}^2$ the elastic modulus is $E = 206000 \text{ MPa}$ and the Poisson ratio is 0.3. The values of the experimental stresses σ_{\max} and τ_{\max} resented in Table 2 were obtained in the study of beams with a corrugated web weakened by perforation.

Table 2. The results of the experimental data.

Loading diagram No.	Total load on the beam ΣQ , kN	The bending moment in the middle of the span M_e , kNm	The transverse force at the supports Q_e , kN	The stress in the flanges σ_{\max} , MPa	The stress in the web τ_{\max} , MPa	Deflection (mm)					
						Y_t B-1	Y_e B-1	Y_c B-1	Y_e^* B-2	Y_c^* B-2	Y_e^* / Y_c^*
1	40	84	20	49.4	12.5	3.41	4	4.28	3.44	5.15	—
2	150	207	75	121.8	47.0	12.8	9.5	12	12.7	13.6	0,93
2	200	276	100	162.4	62.7	17.1	13.2	16	17.1	18.1	0,94
3	250	360	125	211.8	78.3	21.4	18.6	20.5	25.1	23.8	1,05

Analysis of the data in Table 2 shows that the deformation property of the tested B-2 beam in the linear region of behavior $Q_e \approx 0.65\text{--}0.7 Q_{e,\max}$ is 20–30 % larger than that of the similar B-1 beam without weakening, where $Q_{e,\max}$ is maximum experimental load. The value of the relative deflection is $1/430L$. With further loading, the B-2 beams deformation property was 3–50 % higher than the deformation property of the B-1 beam without the perforation. The first group of limit state came when the deflections were equal to $1/225L$.

Comparative analysis of experimental Y_e^* and computer Y_c^* data on deflections for the tested B-2 beam with perforations in loading diagram No. 2 and No. 3 gives a difference in deflections on average no more than 6 %. The data obtained allow using this program as the main one for further numerical studies of corrugated beam with different diameter, type and pitch of perforations in the corrugated web.

According to the above analysis, it can be concluded that stiffening of the web in the areas between the flanges and stiffening element of the perforation by the pair stiffeners is necessary in order to avoid local buckling under the concentrated load in the perforation zone.

2.1. Parametric study of the corrugated beam with different diameter, type and pitch of perforations in the corrugated web

The study of the stress-strain state, the bending moment, the linear analysis of beams with a corrugated metal webs was carried out by various scientists [2–32].

Numerical parametric study of the beam web with corrugation of triangular shape includes analysis of basically 28 models. Of these 28 models, 1 beam the model without web perforations and 27 models with perforations of different sizes and they are located at different distances from each other.

According to above analysis, it is necessary to check the effect of the diameter of $0.25h_w$, $0.5h_w$ and $0.75h_w$ from the web height and the pitch of the perforations with two diameters ($2d$), three diameters ($3d$) and four diameters ($4d$) taken as the distance between the centers of the perforations on the corrugated web with the corrugations of triangular shape operation. The center of the perforations is located in the middle of the web height.

Numerical simulation of the beams was performed using the program LIRA-SAPR, program for the finite element analysis, which includes the requirements for constructions in accordance with EN-1993-1-5:2006 [33]. This program can be used to solve various tasks, from simple linear analysis and on out to complex nonlinear analysis requiring consideration of various manufacturing deviations and material errors. The parametric study was performed for the beam taking into account the various sizes of the perforations in the beam web, distances between the perforations, existence and absents of the perforation stiffening, as well as for the corrugated beam without web perforation. The ability of the beam web with and without the perforation

to withstand the load was considered and an assessment of the effect of web flexibility in accordance with [33] was performed.

For numerical simulation was accepted the beam with a web height $h_w = 840$ mm and a web thickness $t_w = 1.9$ mm. The web corrugations of triangular shape with roundings in the peaks had a wave length $L_r = 350$ mm and a wave height $f_r = 54$ mm (Figure 3). The material of the web and flanges is S245 steel in accordance with Russian State Standard GOST 27772 [28]. The yield strength is $\sigma_y = 245$ N/mm² and the ultimate strength is $\sigma_u = 370$ N/mm².

Finite element models adopted for beams with the corrugations of triangular shape with and without perforations are given in Figure 3.

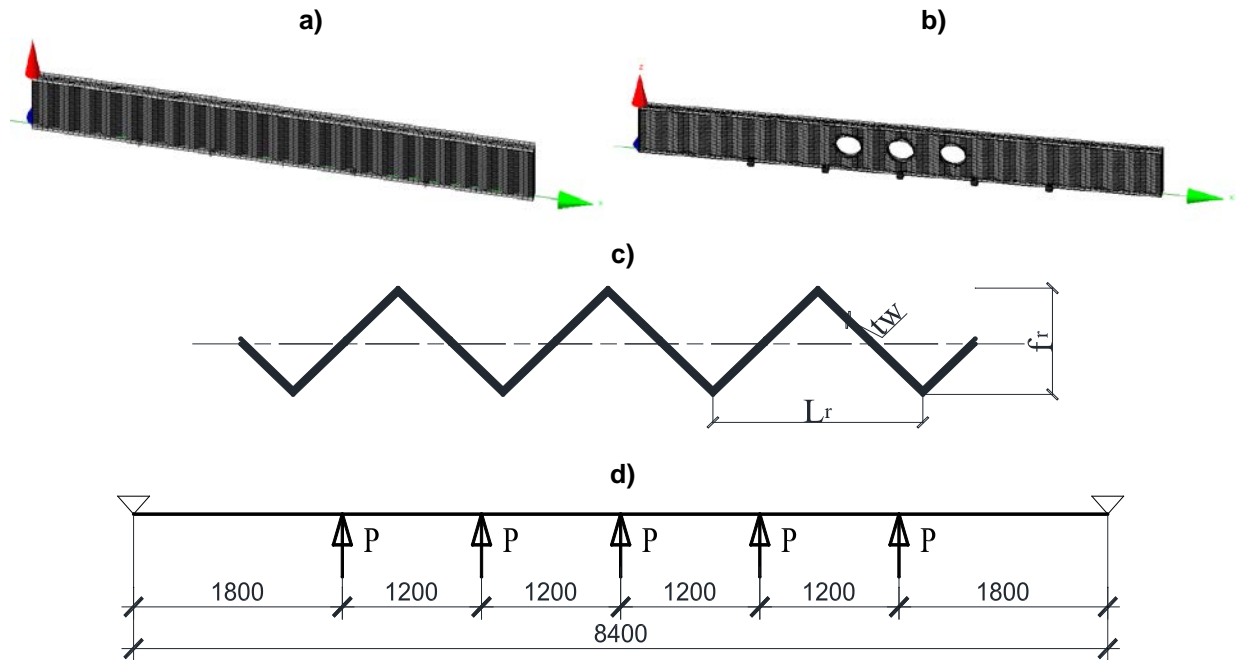


Figure 3. Models adopted for the beams analysis, where a) M-1 corrugated beam with a triangular profile without perforations; b) from M-2 to M-28 corrugated beams with a triangular profile weakened by perforations; c) values of length, height and thickness of web with corrugations of triangular shape adopted in computer simulation; d) model loading diagram for parametric study.

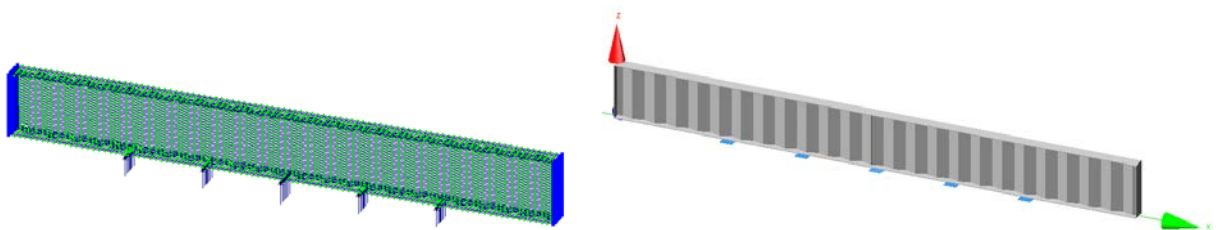
The corrugated beam of constant section (flanges are 200×10 mm, webs are 840×1.9 mm) are made with span of 8400 mm. Two end plates with a thickness $t = 20$ mm is accepted at the ends of each model. Stiffening ring thickness is 3 mm. Paired vertical stiffeners width and thickness is 85×3 mm. Other characteristics of the investigated beams are shown in Table 3.

The load is applied through steel plates of 100×20 mm long equal to the width of the beam flange ($L = 200$ mm), which is in direct contact with the surface of the flange. The load is transmitted at five points from the bottom to the top. The load is applied in the beam center, as well as at a distance from the center in both directions of 1200 mm in accordance with the model loading diagram (Figure 3, 4). The boundary conditions were applied to both ends of the beam model at the nodes of the end plate surface by limiting the required degrees of freedom. The beam at both ends has a fastening along the axes Y and Z .

The tested beam has three circular perforations; the perforations' centers are located in the middle of the web height. The distance between the centers of the perforations is assumed to be $2d$, $3d$ and $4d$ of the perforations. One of the perforations has a constant location in the center of the beam at a distance of 4200 mm from the left and right support to the perforation center. The material of the web and flanges is S245 steel in accordance with GOST 27772 [28]. The yield strength is $\sigma_y = 245$ N/mm², the elastic modulus is $E = 206000$ MPa and the Poisson ratio is 0.3. For the beam models with the length of 8400 mm, the maximum allowable deflection is $1/220L$ or 38.2 mm. Loading (Q) of models is from 50 kN to 350 kN. Loading step is 50 kN. The maximum load value was accepted on the basis of the maximum load that the beam withstood during the experiment. The ultimate strength of the models presented above was studied using finite element analysis.

Table 3. Characteristics of the investigated beams.

Grade of the model	Diameter of the perforation	Stiffening	Perforation pitch	Stiffening ring width (mm)
M-1	without web perforations	—	—	—
M-2	$0.25h_w$	without the perforations stiffening	$2d$	50
M-3	$0.5h_w$	without the perforations stiffening	$2d$	50
M-4	$0.75h_w$	without the perforations stiffening	$2d$	50
M-5	$0.25h_w$	perforation with edging	$2d$	50
M-6	$0.5h_w$	perforation with edging	$2d$	50
M-7	$0.75h_w$	perforation with edging	$2d$	50
M-8	$0.25h_w$	perforation with edging and paired vertical stiffeners	$2d$	50
M-9	$0.5h_w$	perforation with edging and paired vertical stiffeners	$2d$	50
M-10	$0.75h_w$	perforation with edging and paired vertical stiffeners	$2d$	50
M-11	$0.25h_w$	without the perforations stiffening	$3d$	110
M-12	$0.5h_w$	without the perforations stiffening	$3d$	110
M-13	$0.75h_w$	without the perforations stiffening	$3d$	110
M-14	$0.25h_w$	perforation with edging	$3d$	110
M-15	$0.5h_w$	perforation with edging	$3d$	110
M-16	$0.75h_w$	perforation with edging	$3d$	110
M-17	$0.25h_w$	perforation with edging and paired vertical stiffeners	$3d$	110
M-18	$0.5h_w$	perforation with edging and paired vertical stiffeners	$3d$	110
M-19	$0.75h_w$	perforation with edging and paired vertical stiffeners	$3d$	110
M-20	$0.25h_w$	without the perforations stiffening	$4d$	180
M-21	$0.5h_w$	without the perforations stiffening	$4d$	180
M-22	$0.75h_w$	without the perforations stiffening	$4d$	180
M-23	$0.25h_w$	perforation with edging	$4d$	180
M-24	$0.5h_w$	perforation with edging	$4d$	180
M-25	$0.75h_w$	perforation with edging	$4d$	180
M-26	$0.25h_w$	perforation with edging and paired vertical stiffeners	$4d$	180
M-27	$0.5h_w$	perforation with edging and paired vertical stiffeners	$4d$	180
M-28	$0.75h_w$	perforation with edging and paired vertical stiffeners	$4d$	180

**Figure 4. Diagram of model loading.**

3. Results and Discussion

Maximum allowable deflection is not reached when analyzing the obtained data for the M-1 beam model. The deflection for the M-1 beam model under the maximum load effect is 28 mm.

Figures 5–7 show the load-deflection dependence of the middle from M-2 to M-28 beam models with $2d$, $3d$ and $4d$ perforation pitch when operating in the elastic stage. Table 4 shows the shape of deflection of some models.

The Figure 5 shows the load-deflection dependence of the middle from M-2 to M-10 beam models with $2d$ perforation pitch.

The Figure 6 shows the load-deflection dependence of the middle from M-11 to M-19 beam models with $3d$ perforation pitch.

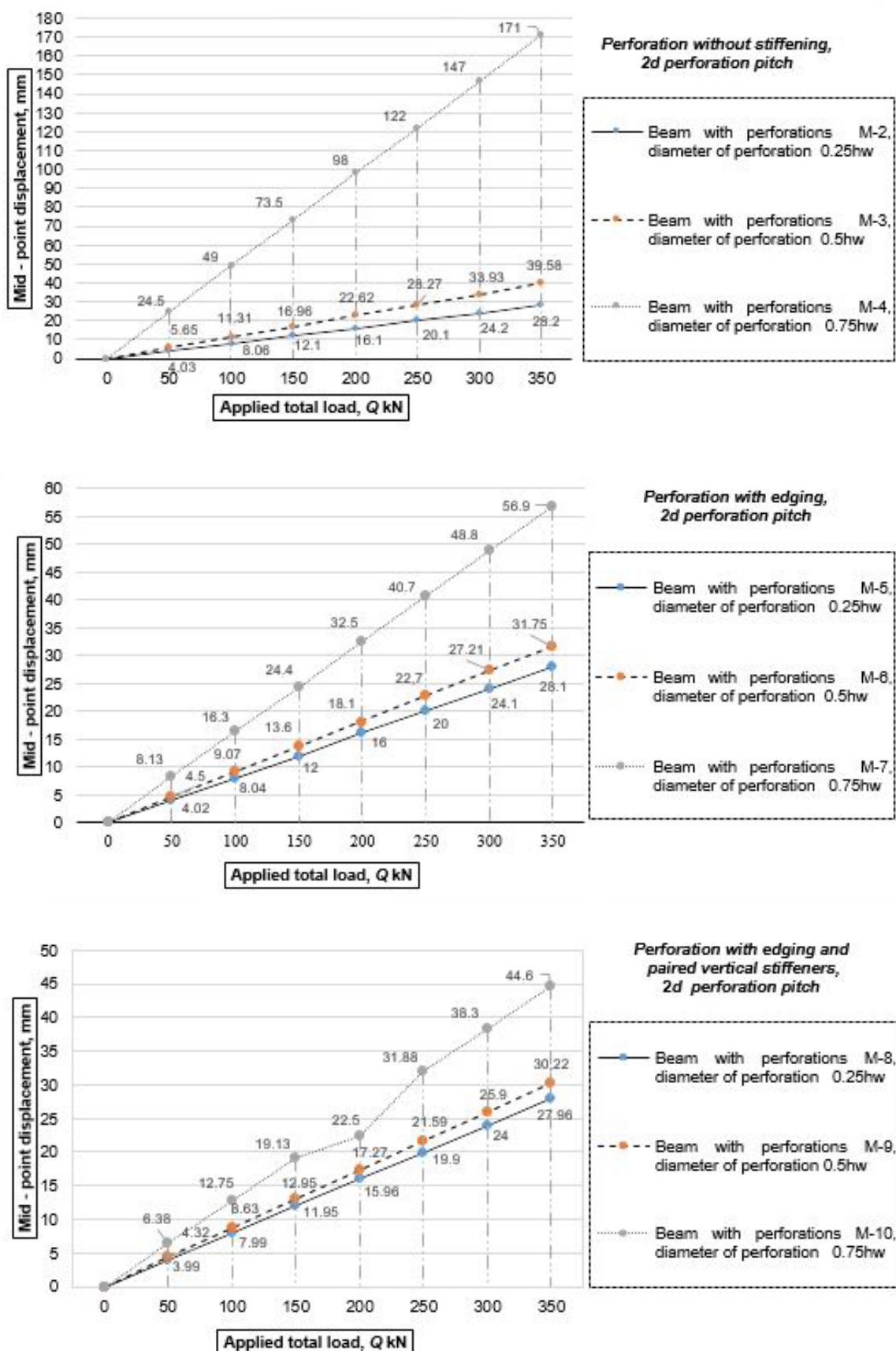


Figure 5. Displacement and applied total load value dependence from M-2 to M-10 beam models with the $2d$ perforation pitch without the perforations stiffening, perforation with edging and perforation with edging and paired vertical stiffeners.

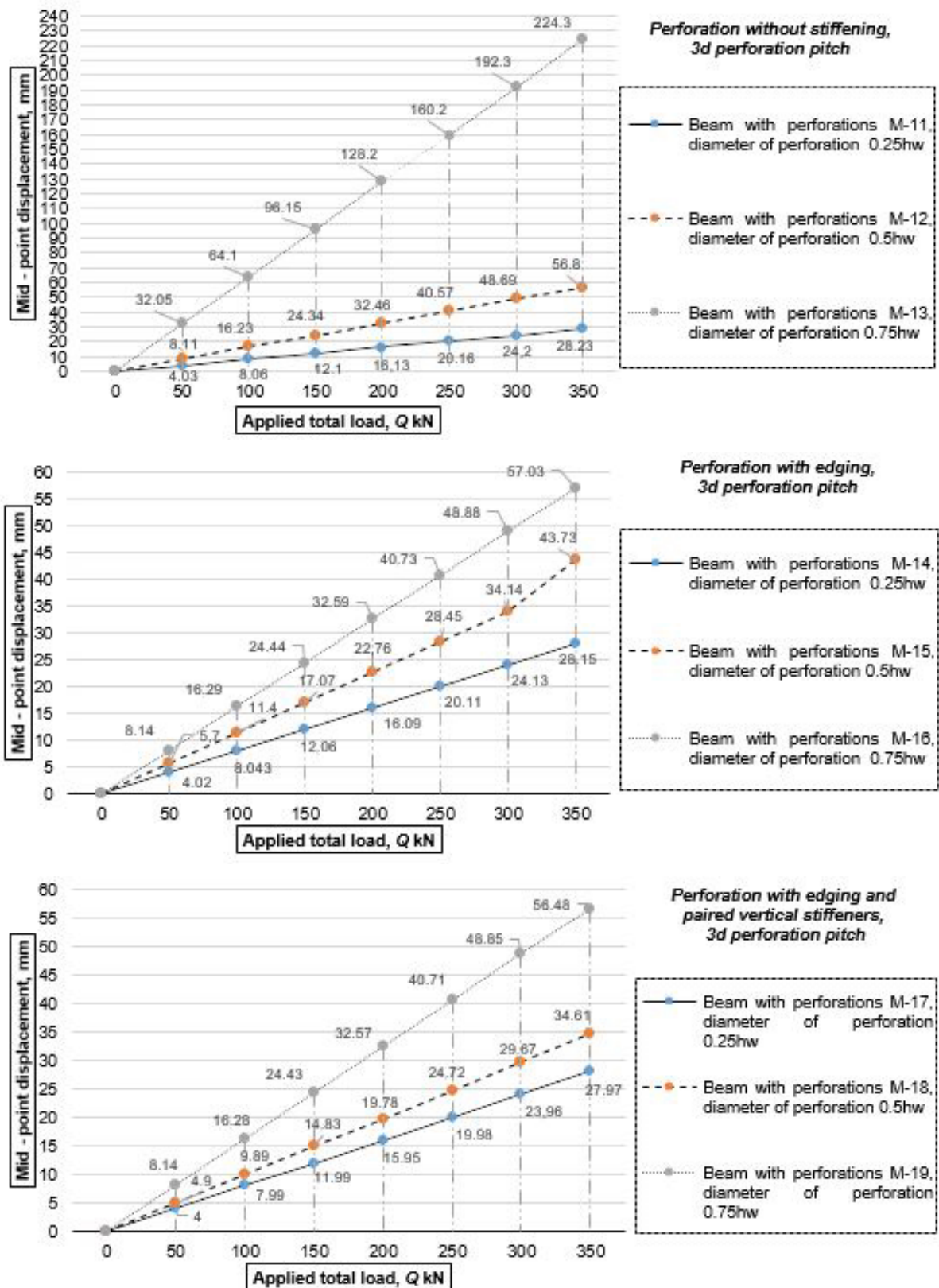


Figure 6. Displacement and applied total load value dependence from M-11 to M-19 beam models with the 3d perforation pitch without the perforations stiffening, perforation with edging and perforation with edging and paired vertical stiffeners.

The Figure 7 shows the load-deflection dependence of the middle from M-20 to M-28 beam models with 4d perforation pitch.

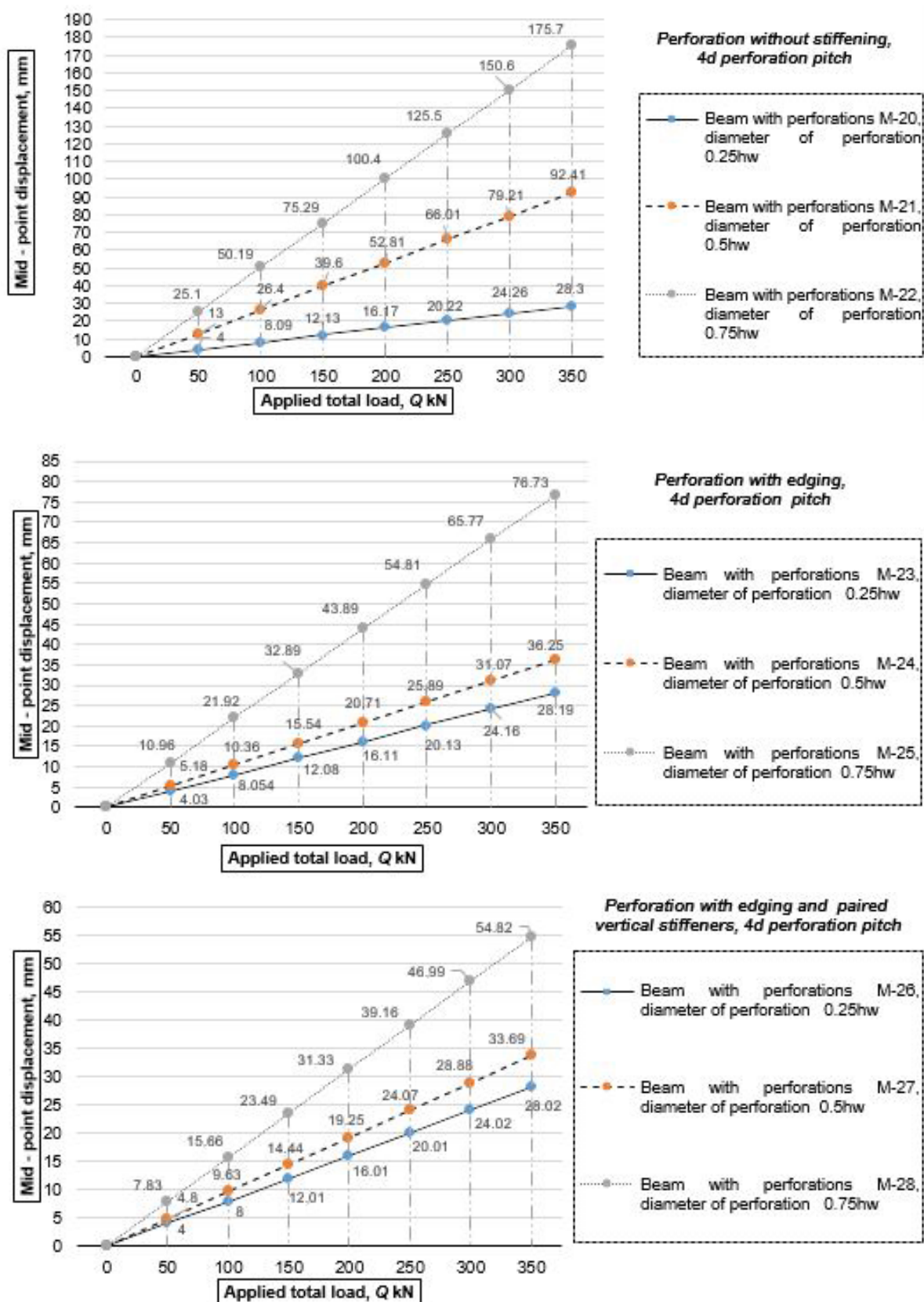





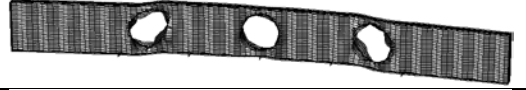
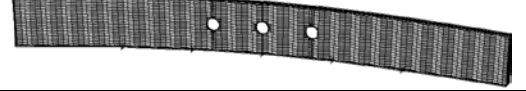
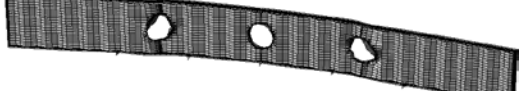
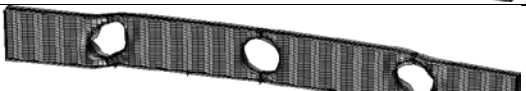


Figure 7. Displacement and applied total load value dependence from M-20 to M-28 beam models with the 4d perforation pitch without the perforations stiffening, perforation with edging and perforation with edging and paired vertical stiffeners

Table 4. Deflection shape of beam models with different diameters and methods of stiffening.

Grade of the Model	Diameter of the perforation	Perforation pitch	Stiffening	Deformation shape
M-2	$0.25h_w$	$2d$	without the perforations stiffening	
M-3	$0.5h_w$	$2d$	without the perforations stiffening	
M-4	$0.75h_w$	$2d$	without the perforations stiffening	
M-14	$0.25h_w$	$3d$	perforation with edging	
M-15	$0.5h_w$	$3d$	perforation with edging	
M-16	$0.75h_w$	$3d$	perforation with edging	
M-26	$0.25h_w$	$4d$	perforation with edging and paired vertical stiffeners	
M-27	$0.5h_w$	$4d$	perforation with edging and paired vertical stiffeners	
M-28	$0.75h_w$	$4d$	perforation with edging and paired vertical stiffeners	

It was decided to begin the analysis of beam models with corrugated web with $2d$ perforations pitch without perforations stiffening to determine the most effective version of the model of corrugated beam with perforations. The obtained data allow to make conclusions that the best result was shown by the M-2 model with a diameter of the perforations of $0.25h_w$ with maximum displacement does not exceeding the maximum permissible one. The deflection of the M-3 beam model with the perforation pitch of $2d$ is greater by 28.8 % than that of the M-2 beam model, and the deflection of the M-4 beam model with the perforation pitch of $0.75h_w$ is greater than that of the M-2 beam model by 510.7 %.

In the same way, the work of other models of beams ranging from M-4 to M-28 was investigated. The results were carefully analyzed; the conclusions are given below.

According to the analysis of beam models with perforations of various diameters and pitches, the following main conclusions can be drawn:

– the most effective model of a beam with the diameter of the perforation of $0.25h_w$ with $2d$ pitch was the M-8 beam model with the actual shearing stress in the section of the corrugated web with the perforation $\tau_{act} \leq 0.1R_s$ under the maximum load effect $Q = 350$ kN, and the maximum possible load Q_{max} on this beam model for achieving the limit deflection is equal to $Q_{max} = 478.2$ kN; with $3d$ pitch was the M-17 beam model with $\tau_{act} \leq 0.14R_s$, and the maximum possible load $Q_{max} = 478$ kN; with $4d$ pitch was the M-26 beam model with $\tau_{act} \leq 0.19R_s$, and the maximum possible load Q_{max} on this beam model for achieving the limit deflection is equal $Q_{max} = 477.2$ kN. All beam models with the perforations stiffened by edging with sheet steel and paired stiffeners located on both sides of the perforation, showed the best results. In the design among these three models of beams, M-8 beam model can be recommend having the best performance with the diameter of the perforation of $0.25h_w$, is minimal, it is recommended to perform them with edging;

– the most effective model of a beam with the diameter of the perforation of $0.5h_w$, with $2d$ pitch was the M-9 beam model with $\tau_{act} \leq 0.29R_s$, and the maximum possible load Q_{max} on this beam model for achieving the limit deflection is equal to $Q_{max} = 442.4$ kN; with $3d$ pitch was the M-18 beam model with $\tau_{act} \leq 0.43R_s$, and the maximum possible load Q_{max} on this beam model for achieving the limit deflection is equal to $Q_{max} = 386.3$ kN; with $4d$ pitch was the M-27 beam model with $\tau_{act} \leq 0.58R_s$, and the maximum possible load Q_{max} on this beam model for achieving the limit deflection is equal to $Q_{max} = 396.8$ kN. All specified models with the perforations stiffened by edging with sheet steel and paired stiffeners located on both sides of the perforation, showed the best results. In the design among these three models of beams, M-9 beam model can be recommend, having the best performance with the diameter of the perforation of $0.5h_w$, and $2d$ pitch;

– the most effective model of a beam with the diameter of the perforation of $0.75h_w$, with $2d$ pitch was the M-10 beam model with $\tau_{act} \leq 0.58R_s$, but the maximum possible load Q_{max} on this beam model for achieving the limit deflection is equal to $Q_{max} = 299.6$ kN; with $3d$ pitch was the M-19 beam model with $\tau_{act} \leq R_s$, under the load of $Q_{max} = 270$ kN; with $4d$ pitch was the M-28 model $\tau_{act} \leq R_s$, under the load of $Q_{max} = 202$ kN. The M-19 and M-29 models with the perforations stiffened by edging with sheet steel and paired stiffeners located on both sides of the perforation showed that the yield point of steel along the shearing stress was reached. When designing, for the listed beam models stiffened by this method, it is not recommended to apply them without additional measures to increase the bearing capacity.

In general, all models showed reduction in resistance of the elements to buckling with increase of the perforation size. Therefore, to decrease the deflections and increase the stability and strength of the beam weakened by the perforations it is necessary to stiffen the perforation. Analysis of behavior of the beam models with perforations under a concentrated load showed reduction of the beam bearing capacity with an increase of the perforations pitch from $2d$ to $4d$ and the diameter of the perforations from $0.25h_w$ to $0.75h_w$. The most optimal diameter of the perforation when designing can be the diameter of the perforation of $0.25h_w$ and $0.5h_w$ with $2d$ or $3d$ perforations pitch. Stiffening the perforation by edging with sheet steel, as well as the perforation stiffening with paired vertical stiffeners is necessary to increase the load-bearing capacity of the corrugated beam weakened by perforations. In the case of an acute need of the perforation with a diameter of $0.75h_w$ it is recommended to use steel with higher strength characteristics in order to increase the bearing capacity and reduce the laboriousness of its manufacture.

In scientific works [17–22], there are no requirements for theoretical and experimental studies on the effect of stiffened perforations on the bearing capacity of the beam with cross-corrugated web with the corrugations of a triangular shape. Therefore, the issue of stiffening of the perforations requires special attention and further studies.

Table 5 shows the result of the obtained deflection data of beam models with corrugated web for perforations with the diameter of $0.25h_w$, $0.5h_w$ and $0.75h_w$ for $2d$ perforations pitch when the perforation is stiffened with ring stiffener and parallel stiffeners with a lip around the exterior circumferential edge of the stiffener ring and without a lip around the exterior circumferential edge of the stiffener ring with different width of the stiffening ring.

The most effective thickness of the edging and stiffeners for the perforation with the diameter of $0.25h_w$, for $2d$ perforations pitch is the thickness of 2 to 4 mm; for the perforation with the diameter of $0.5h_w$, for $2d$ perforations pitch is from 4 to 6 mm; for the perforation with the diameter of $0.75h_w$, for $2d$ perforations pitch is the thickness from 6 to 8 mm.

Figure 8 shows the form for stiffening of beams with corrugated web weakened by circular perforations. Figure 8 (a) shows edging by stiffening ring without a lip around the exterior circumferential edge of the ring and Figure 8 (b) shows edging by stiffening ring with a lip around the exterior circumferential edge of the ring. The ring stiffener provides resistance to web buckling inward.

Figure 9 shows the results of behavior analysis of the M-1 beam models with corrugated web without perforation, the M-3 beam model with the diameter of the perforation of $0.5h_w$ without perforation stiffening, M-6, M-9 beam models with various perforation stiffening options, as well as beam model with elements of the lip around the exterior circumferential edge of the ring stiffener. There is reduction in deflection in all models of beams with perforations stiffened with ring stiffeners of different thickness and width, stiffeners in comparison with models without stiffening. In addition, the deflection reduction was obtained by using a ring stiffener with elements from the lip around the exterior circumferential edge of the ring.

Table 5. Deflections of beams with and without lips.

Grade of the model	Perforation diameter and pitch	Total load, (kN)	Stiffening ring width (mm)	Thickness of stiffening ring and stiffeners without a lip around the exterior circumferential edge of the ring (mm)	Deflection without lip (mm)	Thickness of a lip around the exterior circumferential edge of the ring (mm)	Deflection with lip (mm)
M-8	$0.25h_w, 2d$	350	50	2	28.07	2	28.03
				4	28.01	4	27.96
				6	27.97	6	27.91
				8	27.94	8	27.88
				10	27.91	10	27.86
			75	2	28.06	2	28.04
				4	28	4	27.96
				6	27.96	6	27.91
				8	27.92	8	27.88
				10	27.89	10	27.86
			100	2	28.06	2	28.04
				4	27.99	4	27.99
				6	27.94	6	27.93
				8	27.92	8	27.89
				10	27.92	10	27.86
M-9	$0.5h_w, 2d$	350	110	2	31.32	2	29.17
				4	29.93	4	28.67
				6	29.28	6	28.43
				8	28.89	8	28.27
				10	28.64	10	28.15
			165	2	31.28	2	28.8
				4	29.62	4	28.42
				6	29.05	6	28.24
				8	28.73	8	28.11
				10	28.51	10	28.02
			220	2	31.16	2	28.72
				4	29.39	4	28.38
				6	28.89	6	28.21
				8	28.62	8	28.09
				10	28.43	10	28
M-10	$0.75h_w, 2d$	350	180	2	67.55	2	35.94
				4	44.32	4	32.2
				6	35.85	6	30.89
				8	32.85	8	30.16
				10	31.32	10	29.68
			270	2	69.68	2	33.47
				4	43.62	4	31
				6	34.7	6	30.04
				8	32.03	8	29.49
				10	30.72	10	29.12
			360	2	70.83	2	33.29
				4	42.94	4	30.94
				6	33.84	6	30.01
				8	31.44	8	29.47
				10	30.27	10	29.10

To determine the perforation location effect on the stiffness of the corrugated web with corrugations of triangular shape, it was decided to displacement the center of the perforation by 100 mm towards the tension flange and by 100 mm towards the compressed flange. The diameter of $0.5h_w$ has been adopted as the diameter of the models perforation since the perforation with a diameter of $0.25h_w$ does not have a significant effect on the corrugated web behavior. The $2d$, $3d$ and $4d$ is adopted as considered perforation pitch. The perforation is edged with stiffening ring of 165 mm width, 3 mm thick with the lip around the exterior circumferential edge of the ring, as well as with stiffeners of 10 mm thick. The web thickness was accepted 1.9 mm. The data obtained for the deflection of the models are summarized in Table 6.

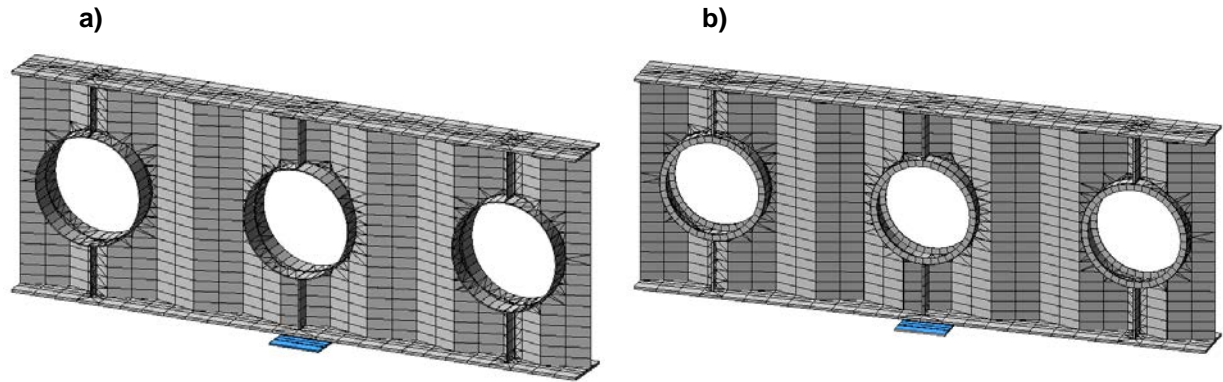


Figure 8. The form for stiffening of circular perforation with the diameter of $0.5h_w$ a) edging by stiffening ring and stiffening without a lip around the exterior circumferential edge of the ring b) edging by stiffening ring and stiffening with a lip around the exterior circumferential edge of the ring

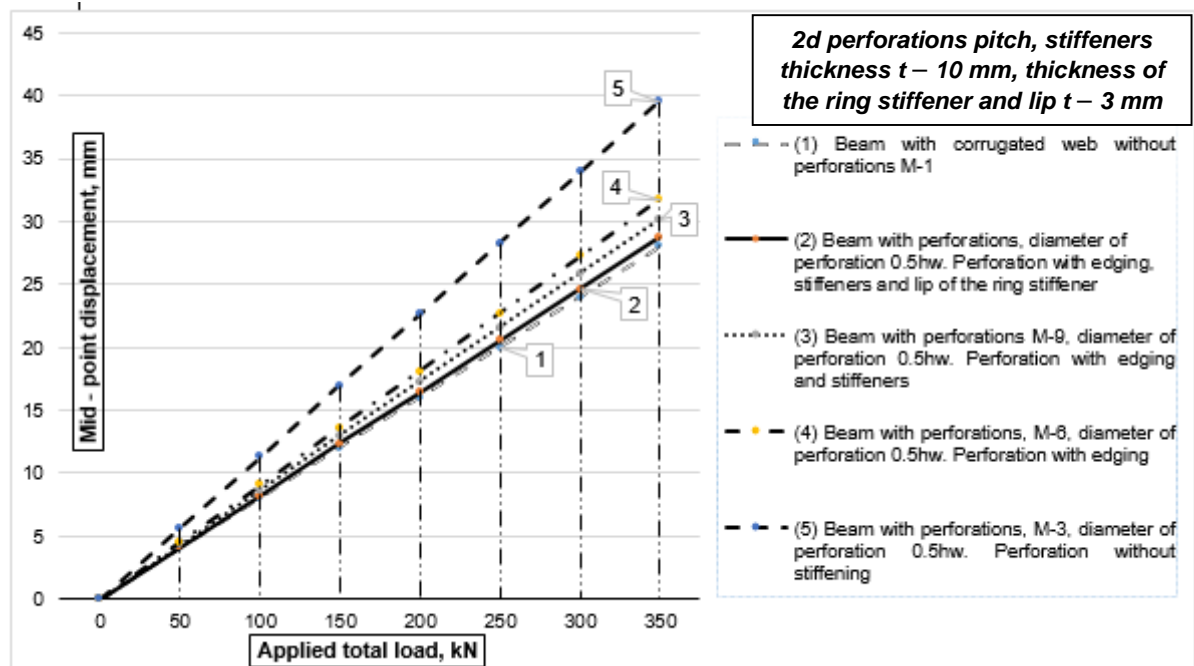


Figure 9. Effectiveness of the perforation stiffening effect on behavior of the beam with corrugated web.

Table 6. The perforation location effect along the height of the corrugated web on the deflection of the beam with stiffened perforations.

Beam model grade	Perforation pitch	Buckling from center to Z axis (mm)	Deflection in (mm) with load in (kN)						
			50	100	150	200	250	300	350
M-9	$2d$	+100	4.04	8.08	12.12	16.17	20.21	24.24	28.29
M-9	$2d$	0	4.08	8.16	12.24	16.32	20.40	24.48	28.56
M-9	$2d$	-100	4.11	8.23	12.35	16.47	20.59	24.71	28.82
M-18	$3d$	+100	4.12	8.24	12.36	16.48	20.60	24.72	28.85
M-18	$3d$	0	4.16	8.33	12.49	16.66	20.82	25.00	29.15
M-18	$3d$	-100	4.22	8.44	12.65	16.87	20.99	25.30	29.52
M-27	$4d$	+100	4.12	8.24	12.36	16.47	20.59	24.71	28.83
M-27	$4d$	0	4.15	8.30	12.45	16.60	20.75	24.90	29.05
M-27	$4d$	-100	4.19	8.34	12.56	16.75	20.94	25.13	29.32

Analyzing the data of Table 6, it can be concluded that the least deflection of beam models with diameter of the perforation of $0.5h_w$ was obtained with the $2d$ perforations pitch. In all three cases of a different perforations pitch, the buckling of the perforation in direction of the tension or compressed flange did not significantly affect the deflection. However, it can be noted that a slight reduction in the deflection of the models is achieved by buckling the perforation in the direction of the tension beam flange. This gives grounds to state that the central part of the web is the most optimal option for the perforation location along the height of the

beam web, but in cases where it is necessary to displacement the perforation, it will be more effective to displacement towards the tension flange of the beam with corrugated web.

4. Conclusions

The undertaken study and the obtained results lead to the following conclusions:

1. Stiffening of the web and perforation by the pair stiffeners is necessary in order to avoid local buckling under the concentrated load in the perforation zone.
2. A numerical parametric study of a beam with corrugation of triangular shape showed the efficiency of perforations location in the corrugated web with the $2d$ perforation pitch and with the diameter of the perforation of $0.25h_w$, $0.5h_w$ and $0.75h_w$ stiffened with ring plates and parallel stiffeners.
3. The reduction in deflection in all models of beams with perforations stiffened with ring stiffeners of different thickness and width, stiffeners in comparison with models without stiffening has been found.
4. The deflection reduction has been reached by using a ring stiffener with elements from the lip around the exterior circumferential edge of the ring.
5. The most effective location of the perforation along the web height has been determined, which can also be used as a guide during decision making process of beam perforations in general.

The findings showed that the optimized perforation needs to be less than half of the beam height, while the central part of the web is the most optimal option for the perforation location along the height of the beam web and most efficiency distance between the perforations is $2d$ perforation pitch.

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Влияние отверстий на деформативность стенки сварной гофрированной балки

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Ключевые слова: балка с гофрированной стенкой, отверстие в стенке, треугольное очертание гофр, прогиб балки, анализ методом конечных элементов, кольцевой усилитель

Аннотация. При проектировании некоторых объектов возникает необходимость устройства в гофрированных стенках балок отверстий различного диаметра для пропуска технологического оборудования в пределах строительной высоты балки, хотя это снижает несущую способность стенки. Отсутствие информации о характере работы, величинах критических напряжений, устойчивости гофрированных стенок балок, ослабленных отверстиями, вызвало необходимость проведения соответствующих исследований, для которых в стенках балок были образованы отверстия различного диаметра и с различными способами их подкрепления. Данное исследование, решает несколько задач: анализ работы сварных двутавровых балок с гофрированными стенками треугольного очертания, ослабленных технологическими отверстиями различного диаметра и различного расстояния между отверстиями на несущую способность; определяется влияние отверстий на способность воспринимать поперечную нагрузку, рассматриваются способы усиления отверстий. Приводится анализ влияния толщины окаймления, парных вертикальных ребер жёсткости при различной ширине кольцевого усилителя на работу моделей балок с гофрированной стенкой с отверстиями. Определено влияние загиба внешней грани кольцевого усилителя на несущую способность балок с гофрированной стенкой ослабленных отверстиями, а также наиболее эффективное месторасположение отверстия по высоте стенки, при проектировании.

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